

# UNUSUAL ASPECTS TO BE CONSIDERED IN THE SIMULATION OF POSITIVE DISPLACEMENT MACHINES

**Massimo Rundo**



**POLITECNICO  
DI TORINO**

Dipartimento  
Energia



Fluid Power  
Research Laboratory



**CCEFP Summit at Purdue in Honor of Monika Ivantysynova**

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# Summary

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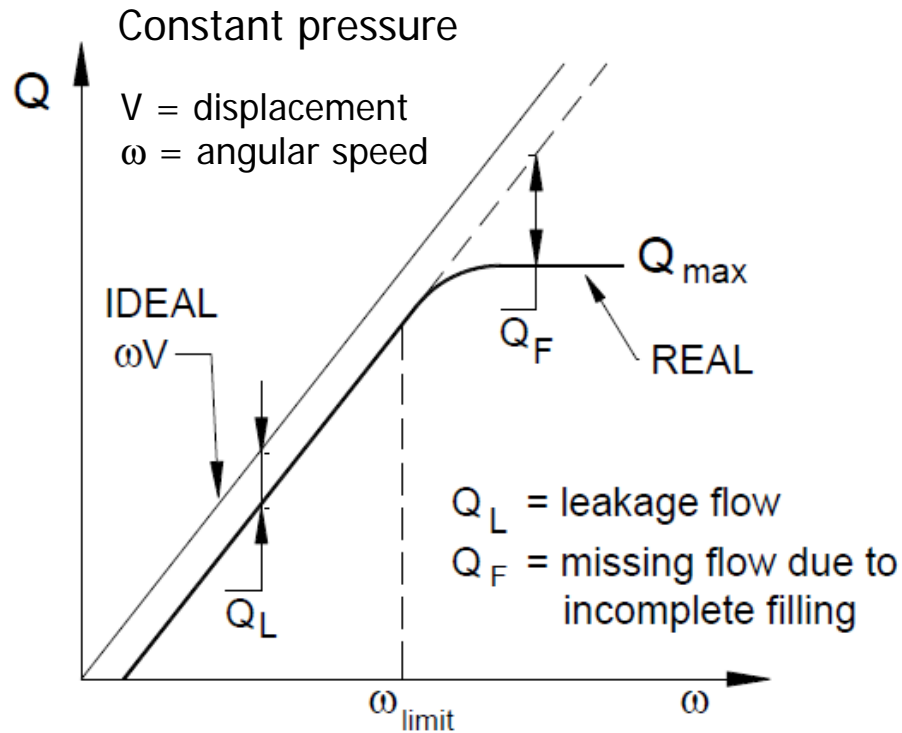
## 3 EXAMPLES ANALYZED

- **Centrifugal force on the oil in the variable chambers in conditions of incomplete filling**
- **Elastic deformation of the cover/port plate**  
Positive or negative effects on:
  - **volumetric efficiency**
  - **pressure ripple**
- **Elastic deformation of the stator**  
Influence on the pump displacement

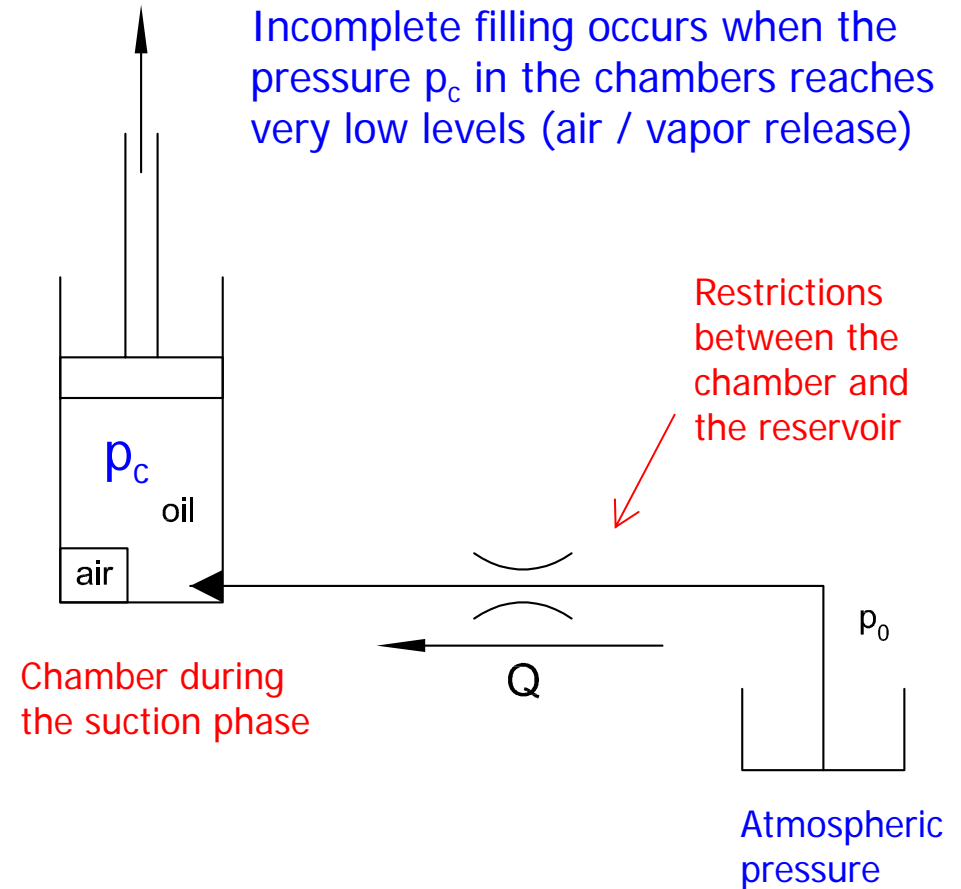


# Incomplete filling

In a positive displacement pump, the real flow rate  $Q$  differs from the theoretical value due to the leakages and, at high speed, to the incomplete filling

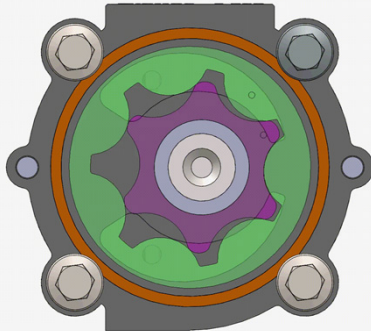


Incomplete filling occurs when the pressure  $p_c$  in the chambers reaches very low levels (air / vapor release)

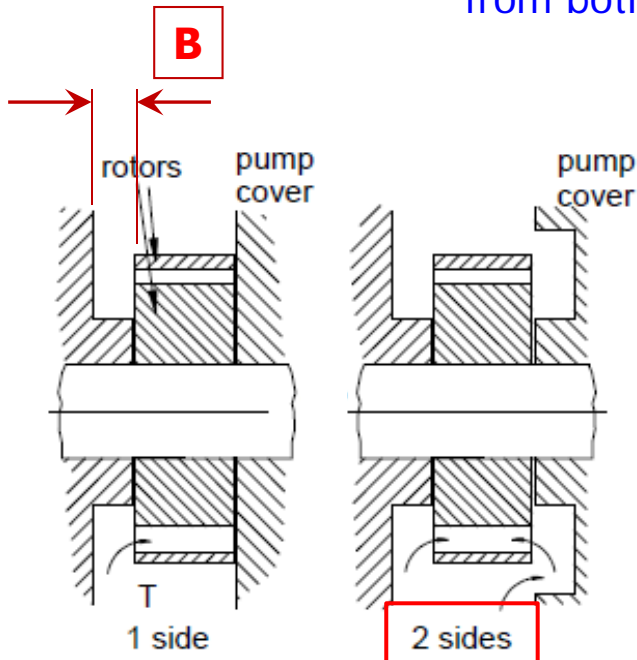


# Common remedies for improving the filling

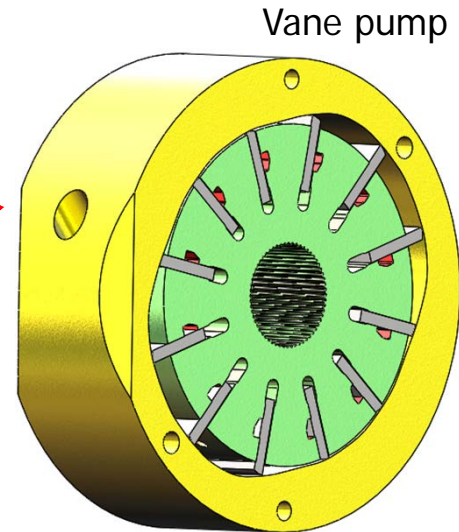
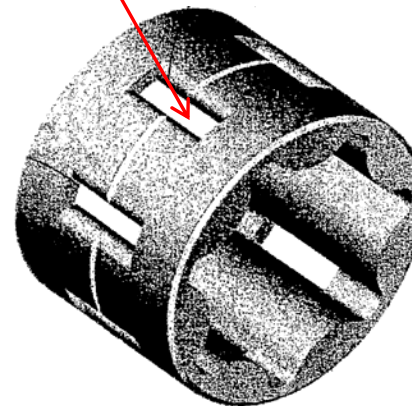
- Reduction of the pressure drop in the suction pipe
- Increment of the chambers' flow areas ...



... by feeding the chamber from both sides



... by feeding radially through holes, slots, cuttings

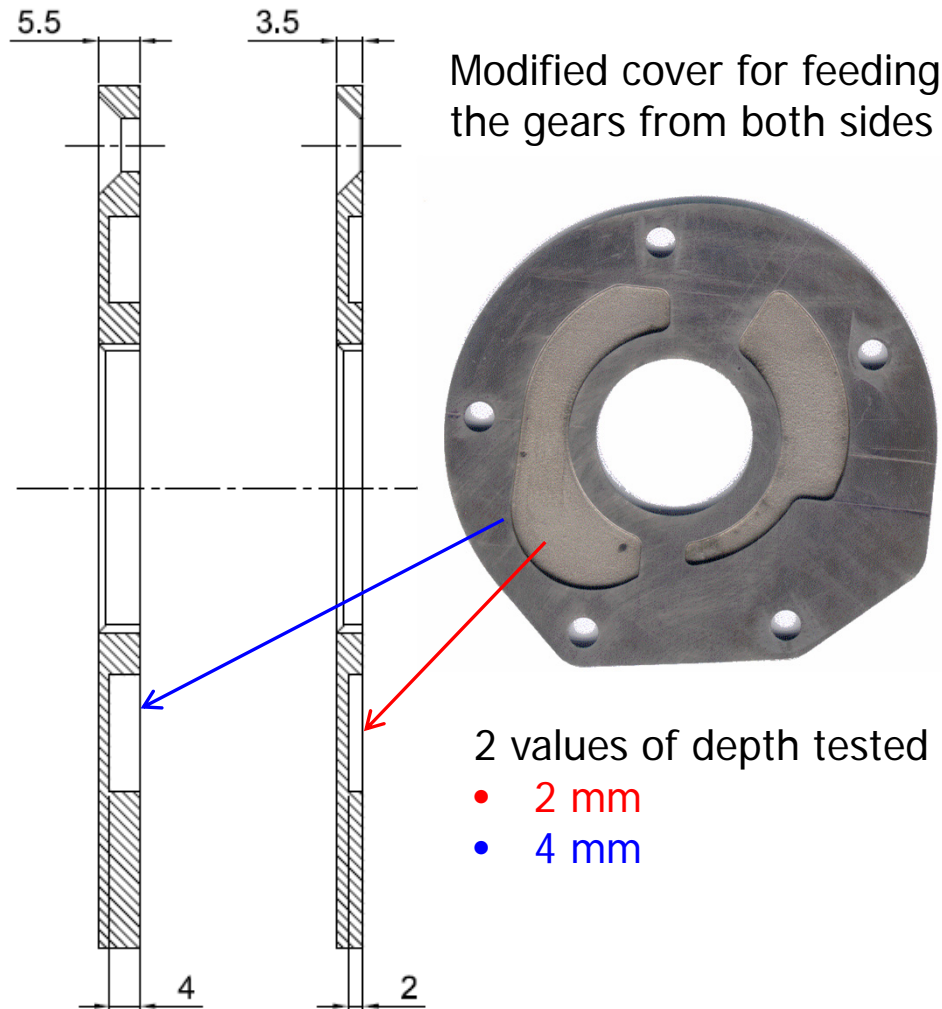


Outer rotor of internal gear pump

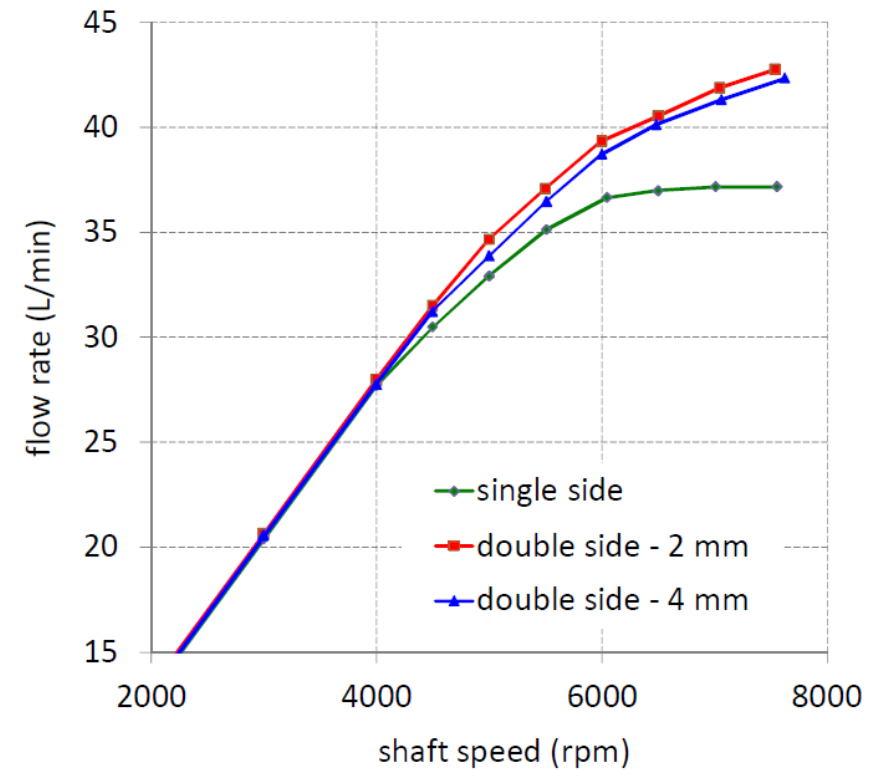
**Not always these solutions are beneficial !**



# Former «unexplained» experience on gerotor



Experimental flow-speed curves (23 February 1999)

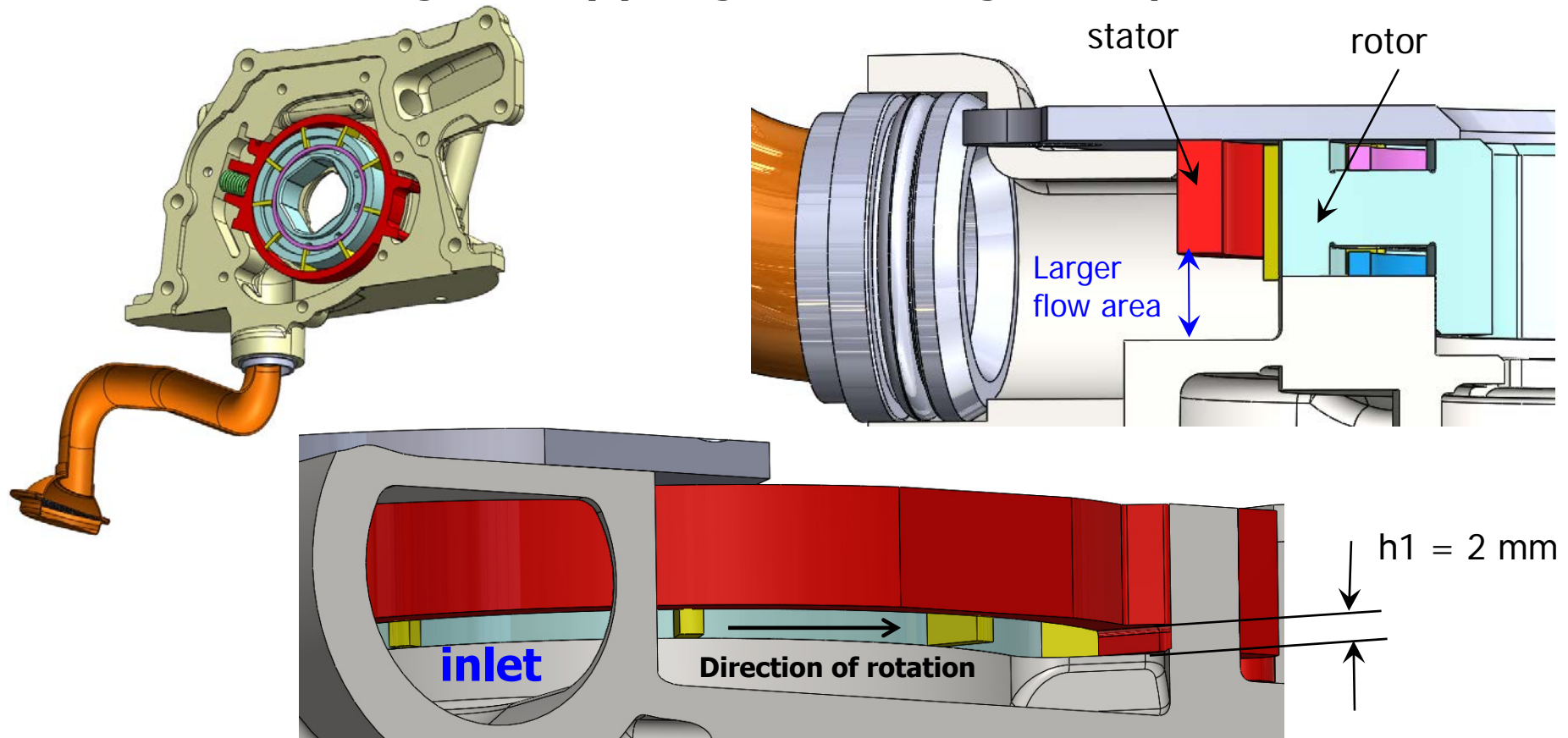


**From 2 to 4 mm → worsening (!?)**



# Similar experience on a vane pump

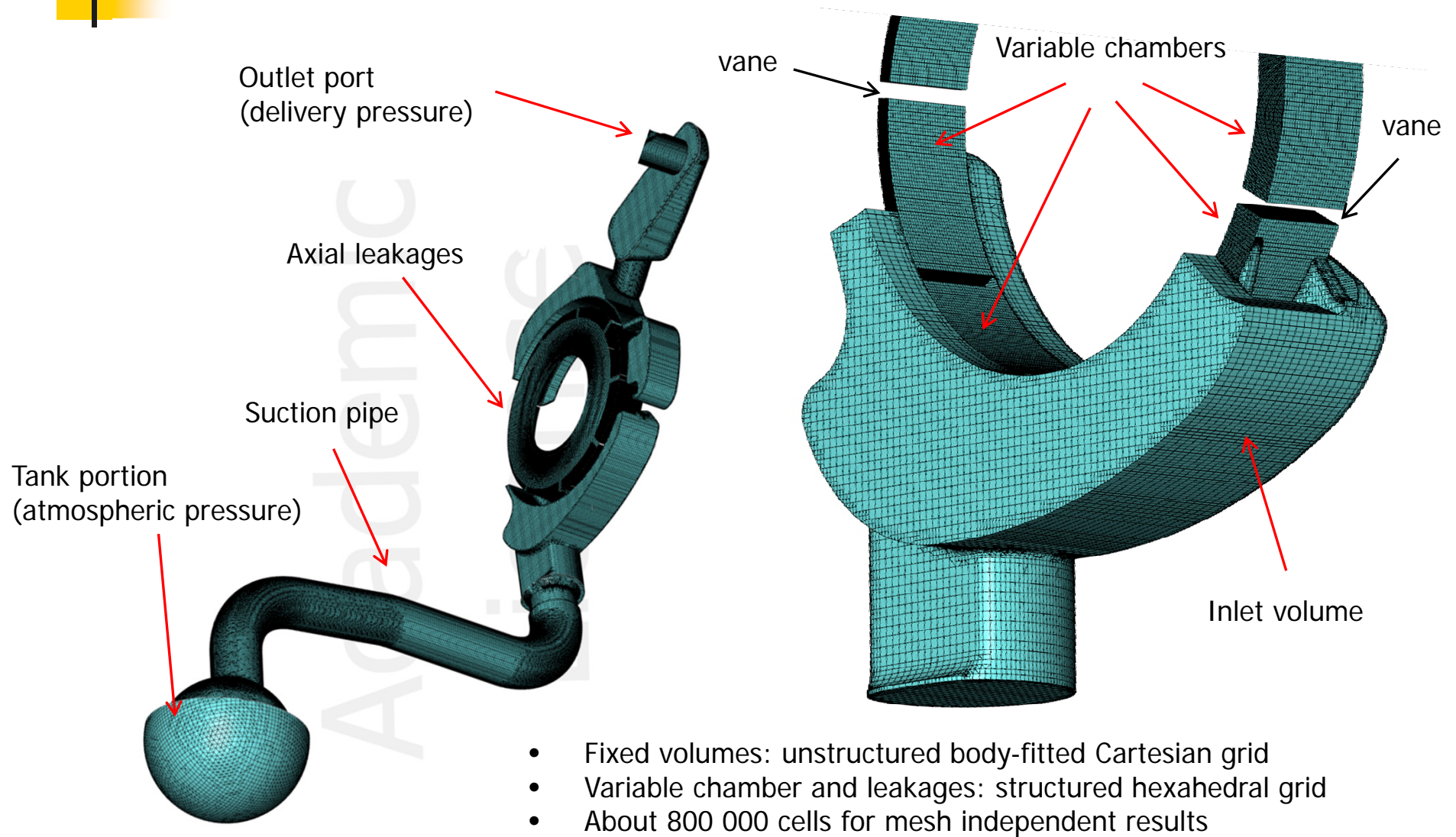
**Baseline configuration (1): single side feeding with improved flow area**



Experimental tests and CFD simulations have demonstrated the effectiveness of the milling  $h_1$



# CFD model of the reference pump

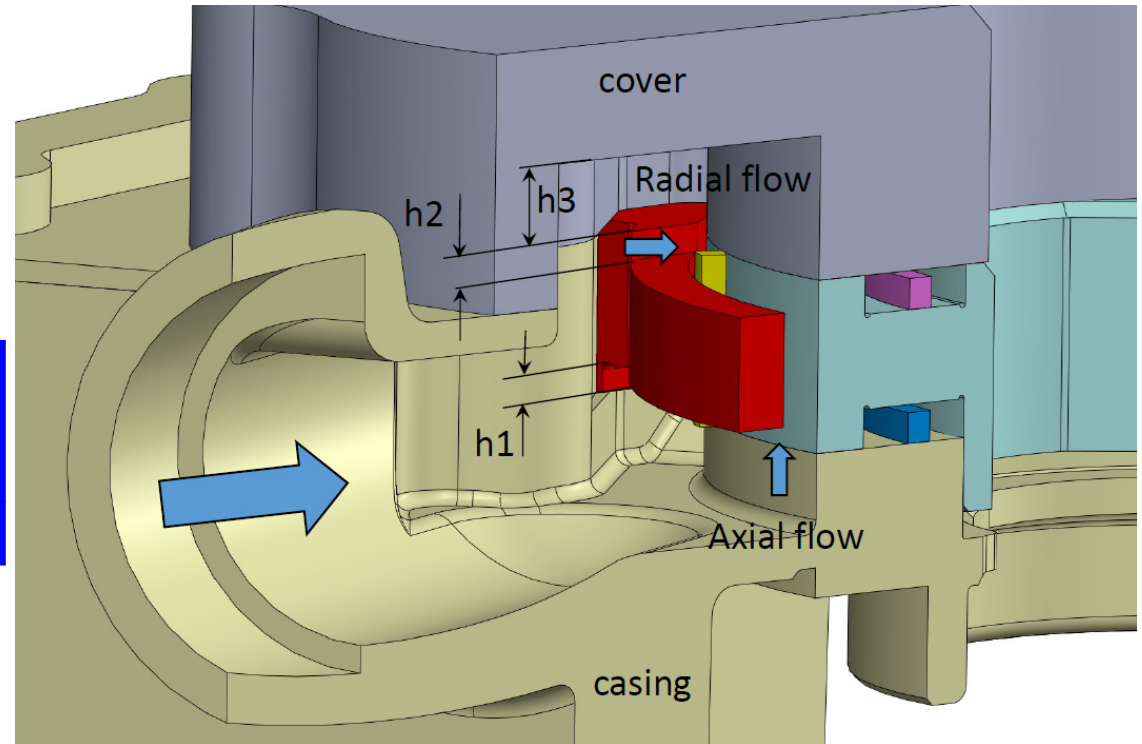


# Five configurations analyzed

CFD simulations at :  
5200 rpm – displacement 55%

$h_1 = 2 \text{ mm}$

Config.	$h_2$ (mm)	$h_3$ (mm)	Flow rate (L/min)
1	0	0	40.1
2	1	0	37.4
3	2	0	33.2
4	0	5	37.4
5	2	5	35.4



With OD model any additional flow area causes the increment of the flow rate

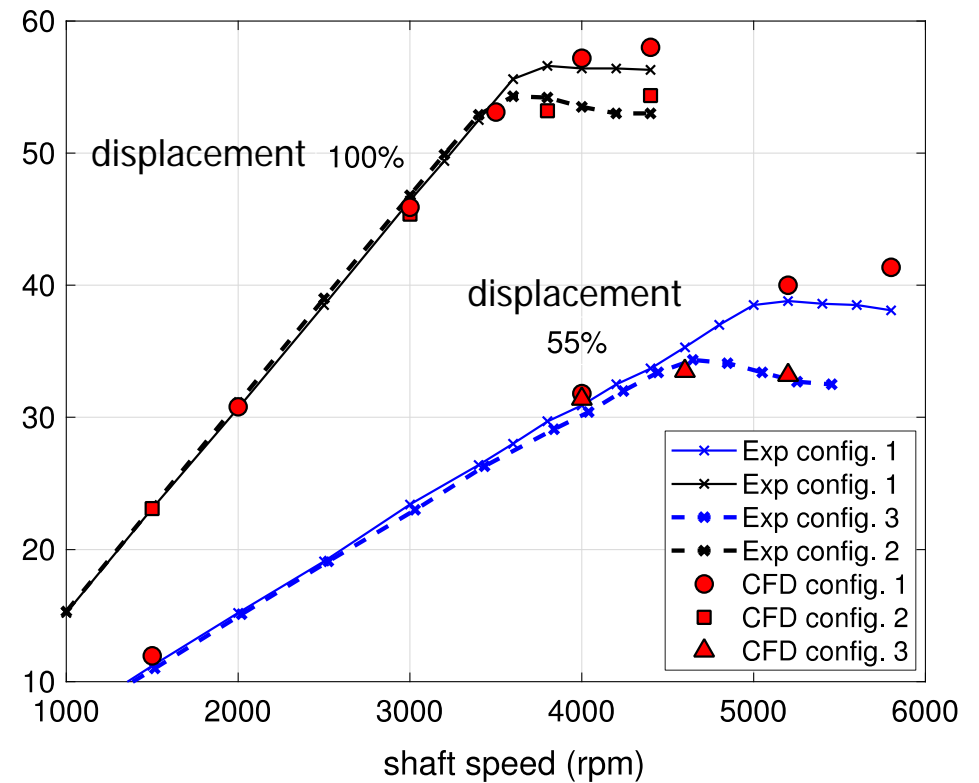
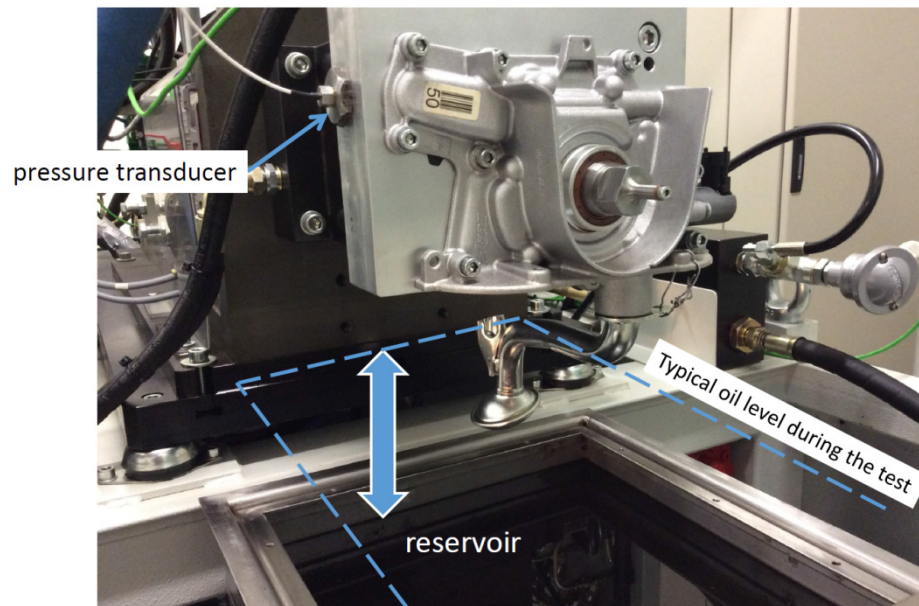
**The 3D model gives opposite results (higher area = lower flow rate)**



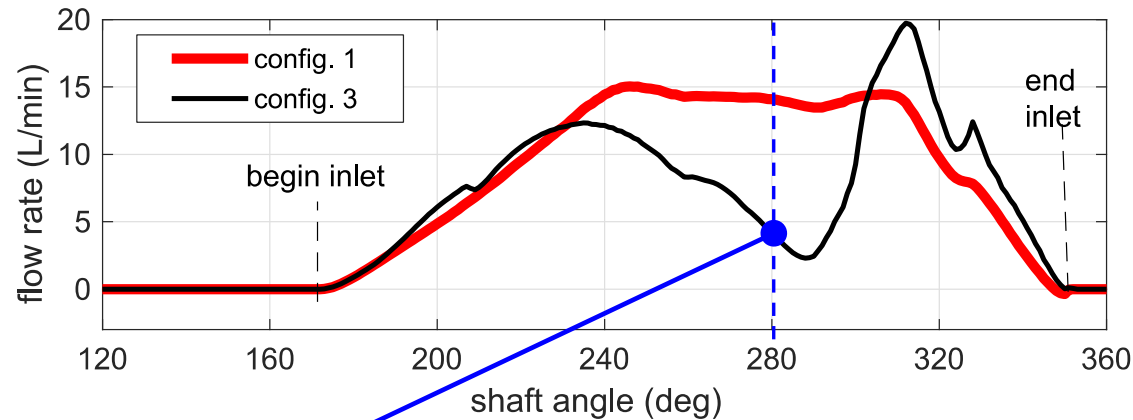


# Model validation

Constant delivery pressure (3 bar)  
and constant displacement

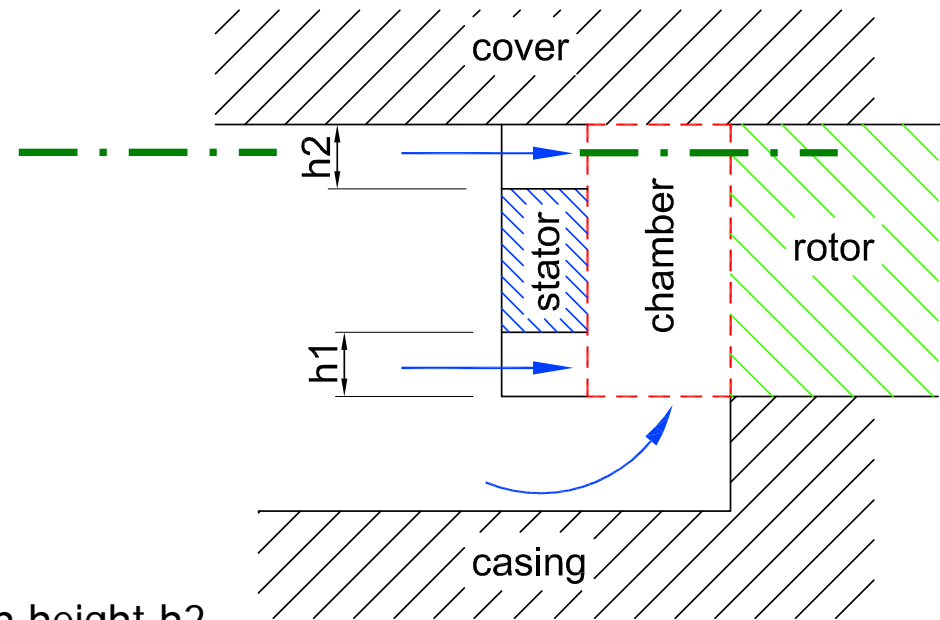
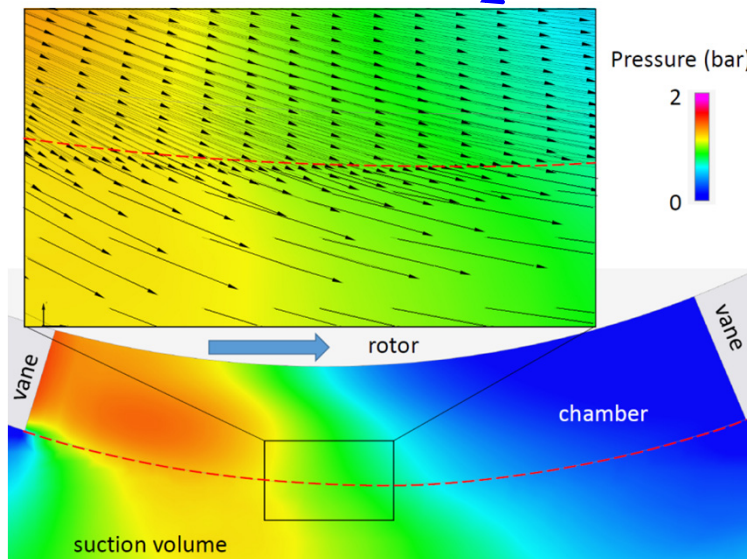


# Flow rate entering a chamber: configs 1 & 3



(5200 rpm – 55% displ.)

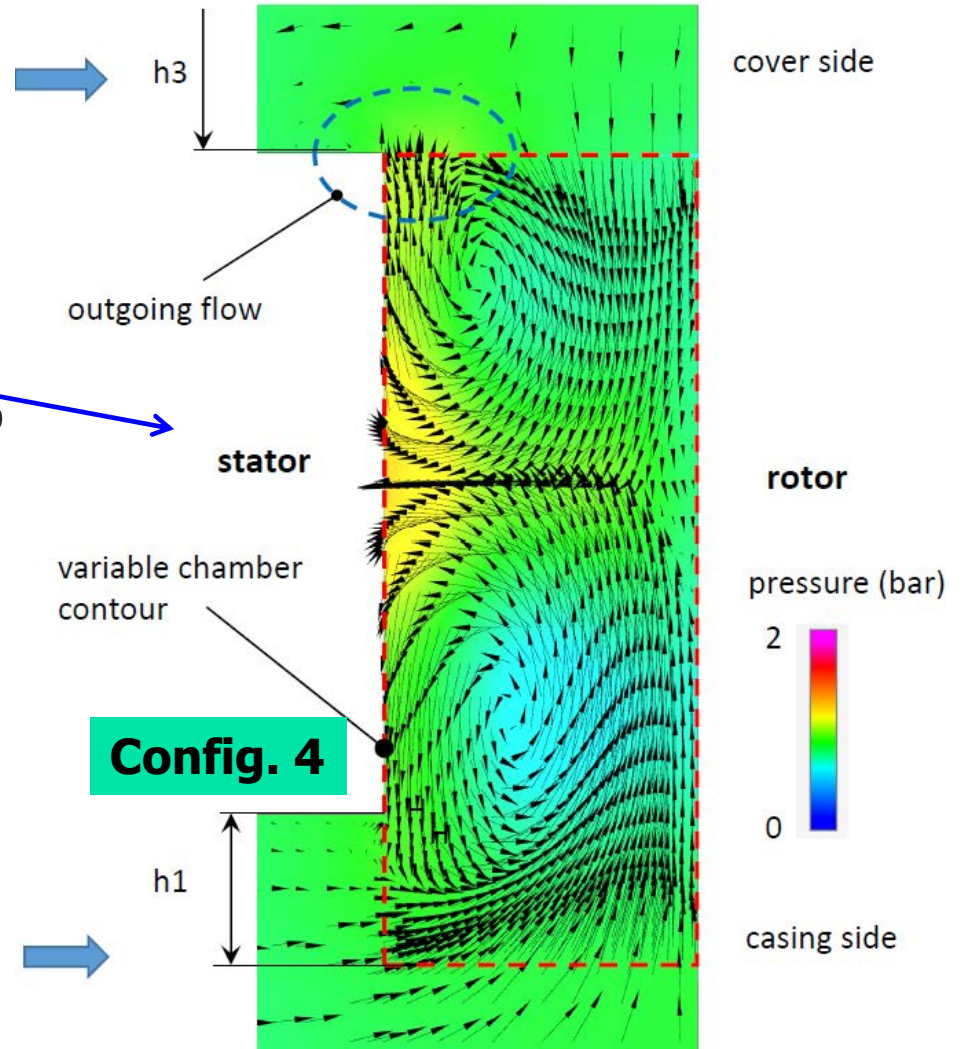
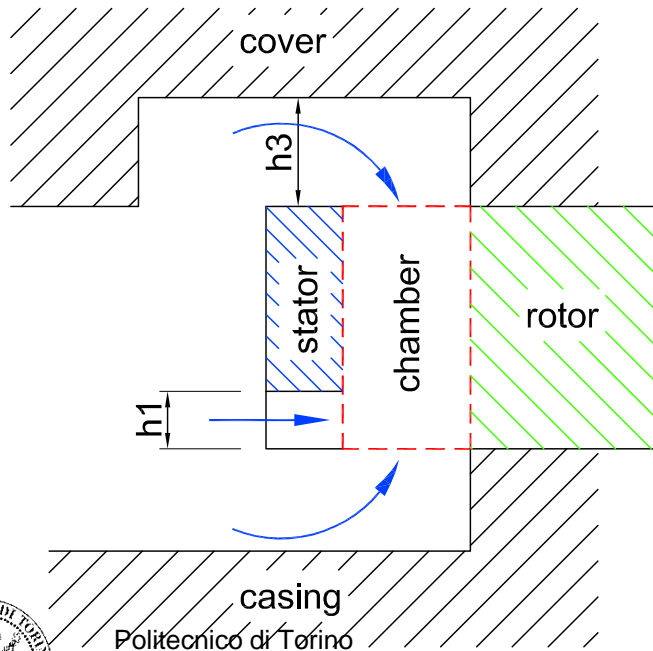
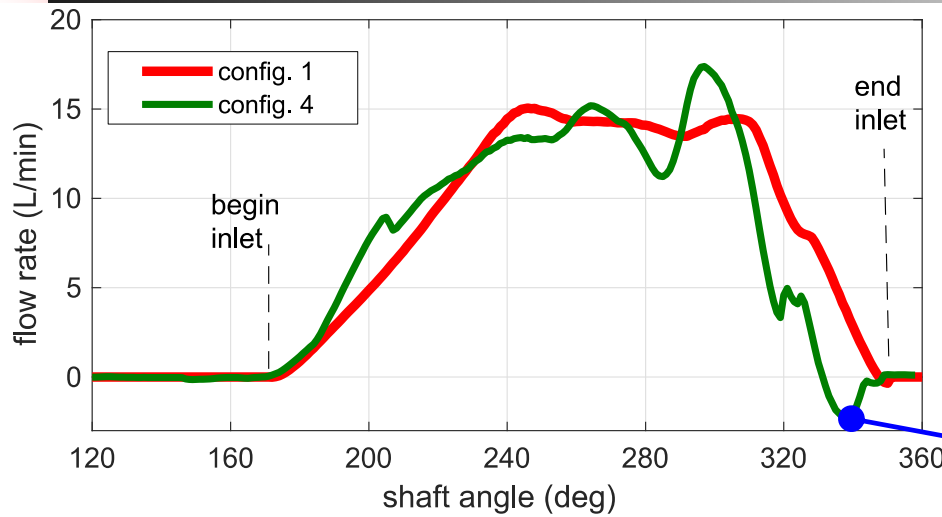
**Config. 3**



Cut plot in the middle of the milling with height  $h_2$



# Flow rate entering a chamber: configs 1 & 4





# Some intermediate remarks

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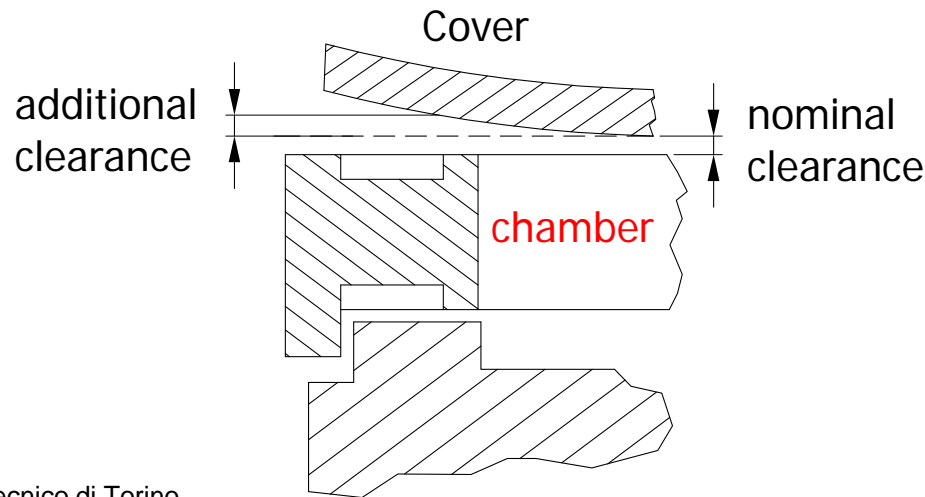
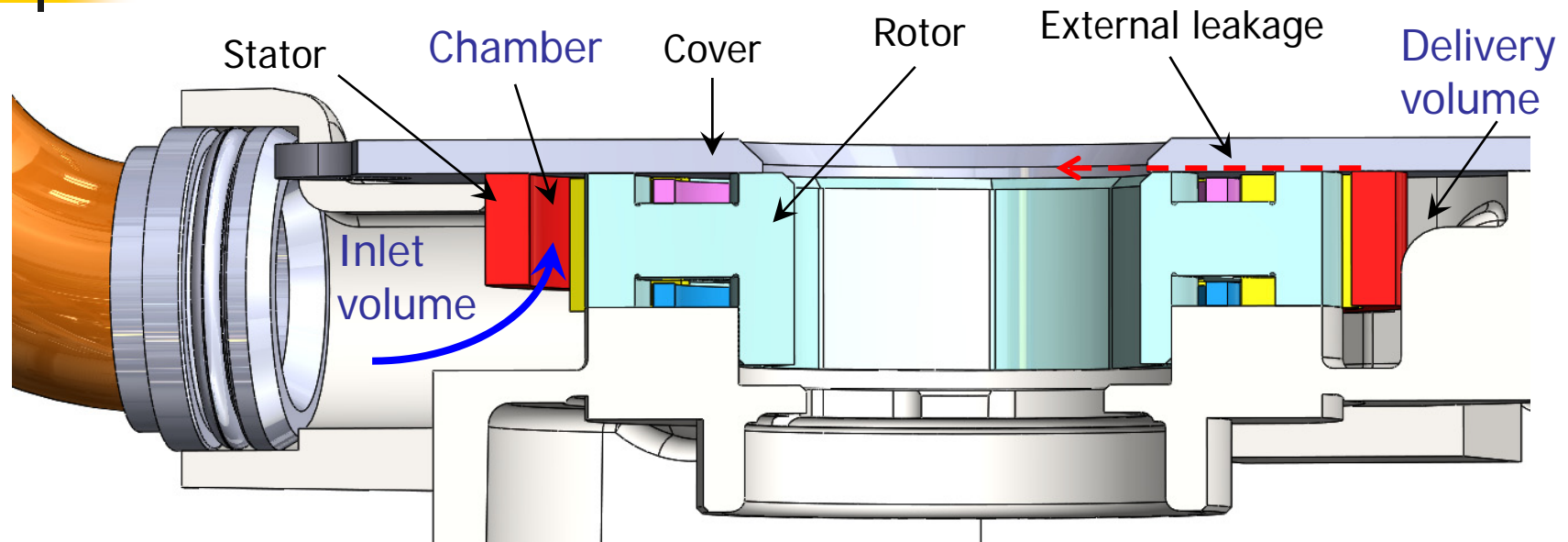
- In pumps with high ratio thickness/diameter both double feeding and radial feeding through slot in the stator are beneficial (as expected)
- In pumps with low ratio thickness/diameter the effect of centrifugal force is predominant above all at low displacement

→ Unusual aspect to be considered:

**centrifugal force in the variable chambers**



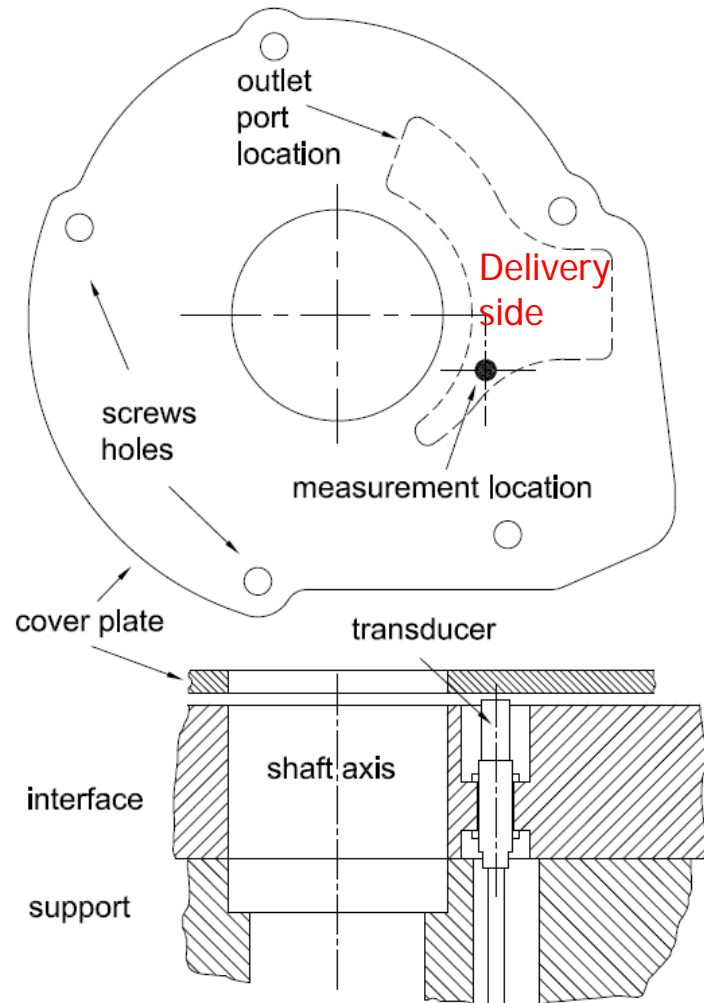
# Influence of cover deformation



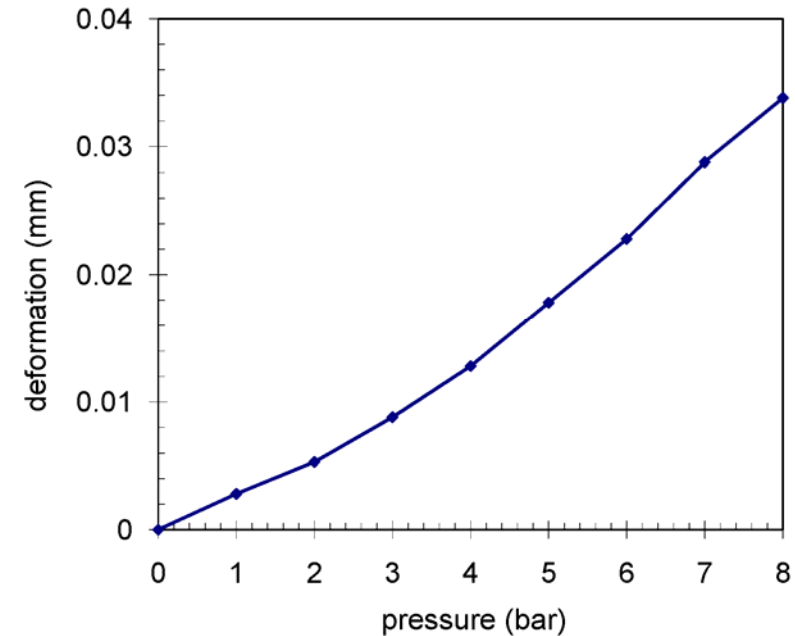
**Is it so important ?**



# Measurement of the additional gap



Output of contactless displacement transducer



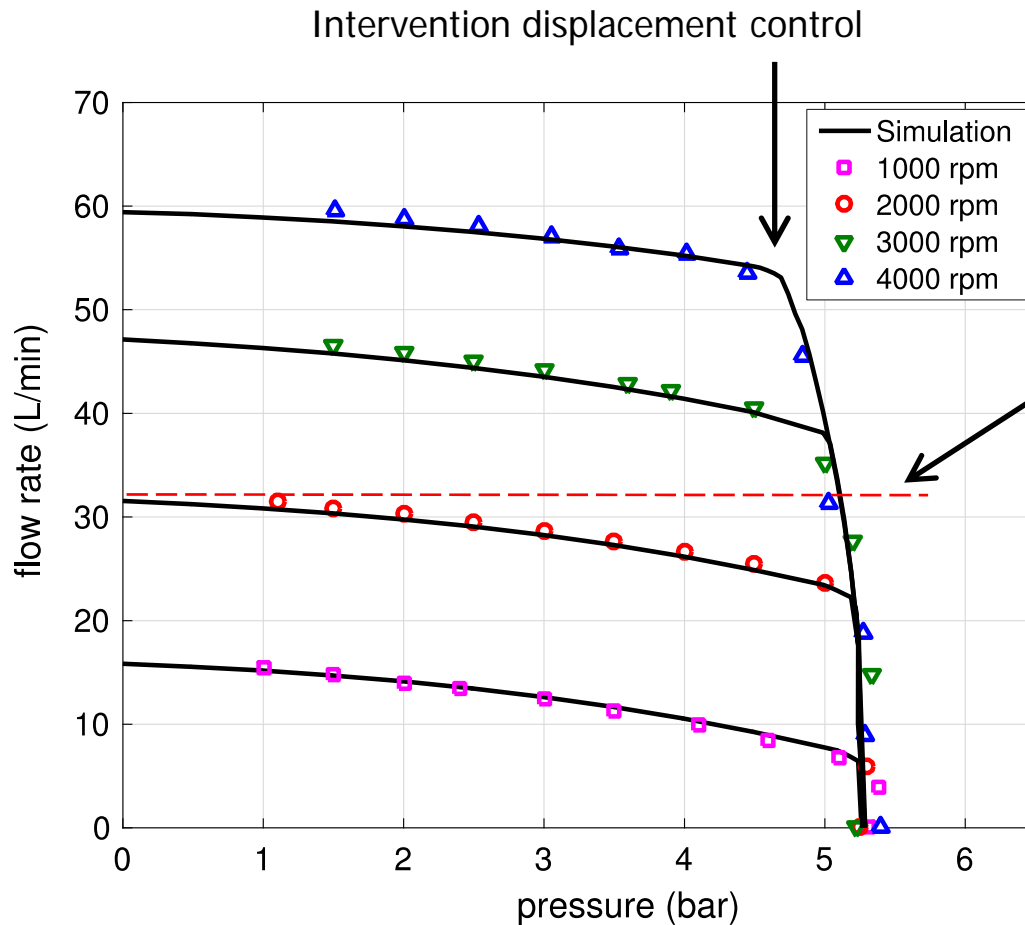
Nominal gap 20-30  $\mu\text{m}$   
Additional gap 8 bar 35  $\mu\text{m}$

-> external leakage = 10 times higher !!



# Steady-state flow-pressure curves

0D model with coefficient tuned on FEM



Oil temperature: 120 °C

**Progressive reduction of flow area of the load valve**

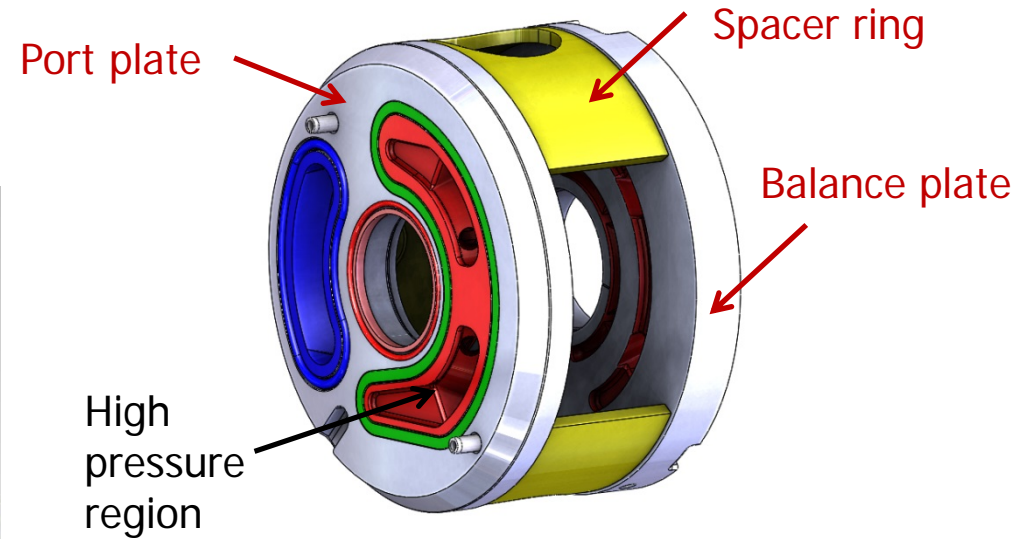
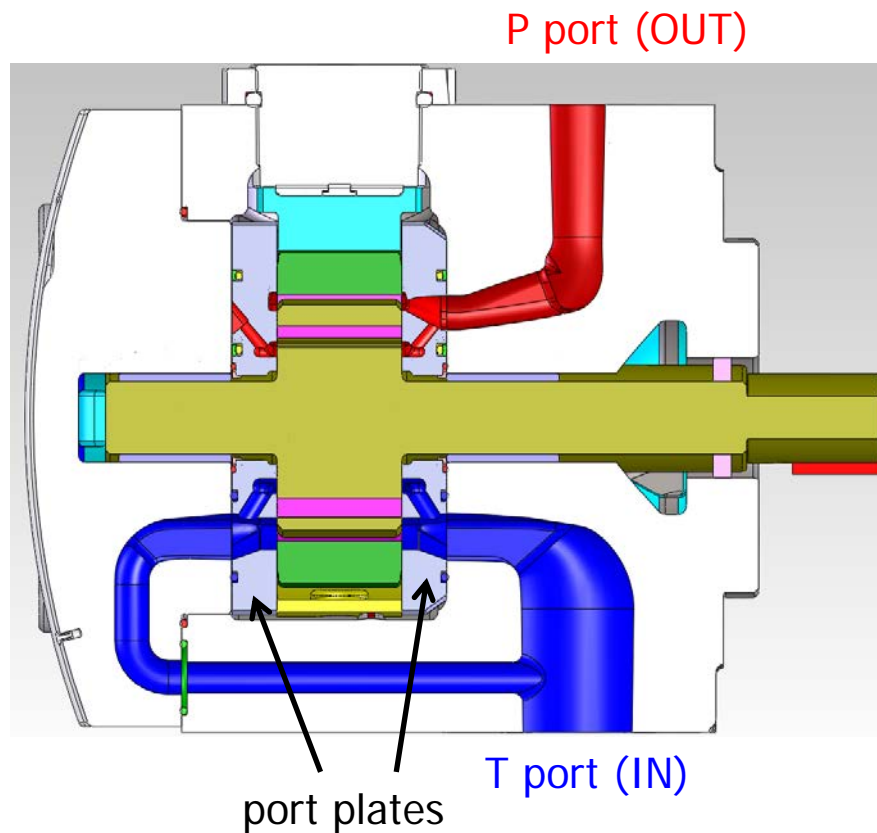
Theoretical flow rate

Non-linear flow-pressure characteristic due to the variable clearance (deformation of the cover)

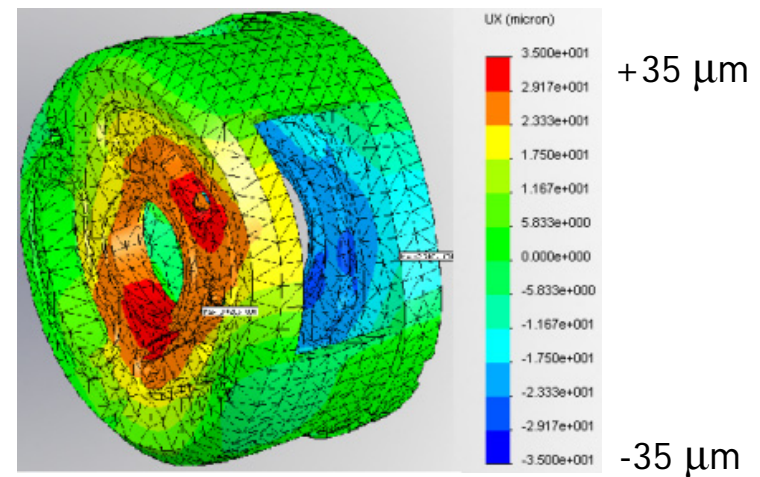
$$Q_{leak} = \frac{b(h + k \cdot p)^3}{12\mu L} p$$



# The case of high pressure vane pump

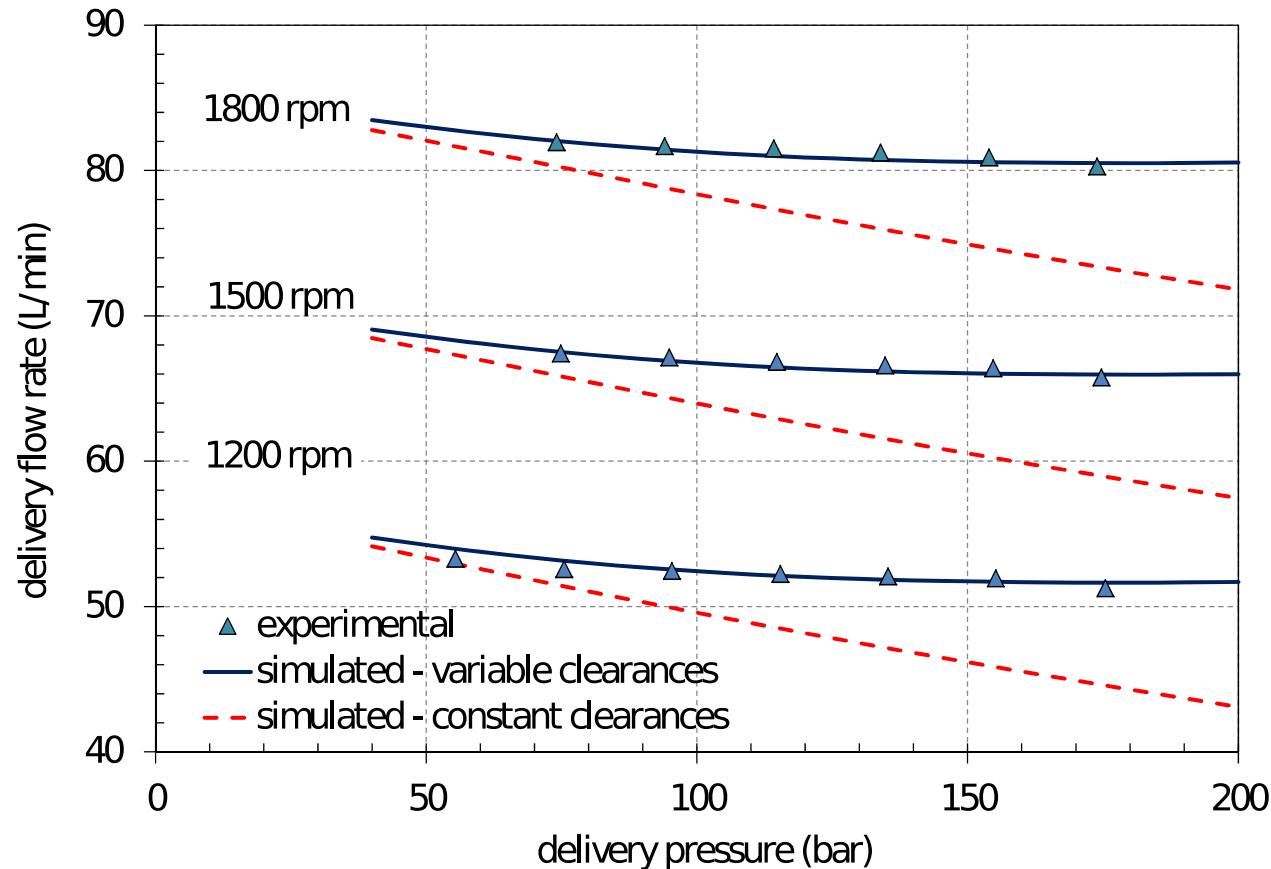


Deformation field at 200 bar





# ... and the effect of the port plate deformation



Non-linear flow-pressure characteristic due to the variable clearance (deformation of the port plate)

Nominal clearance

gap width

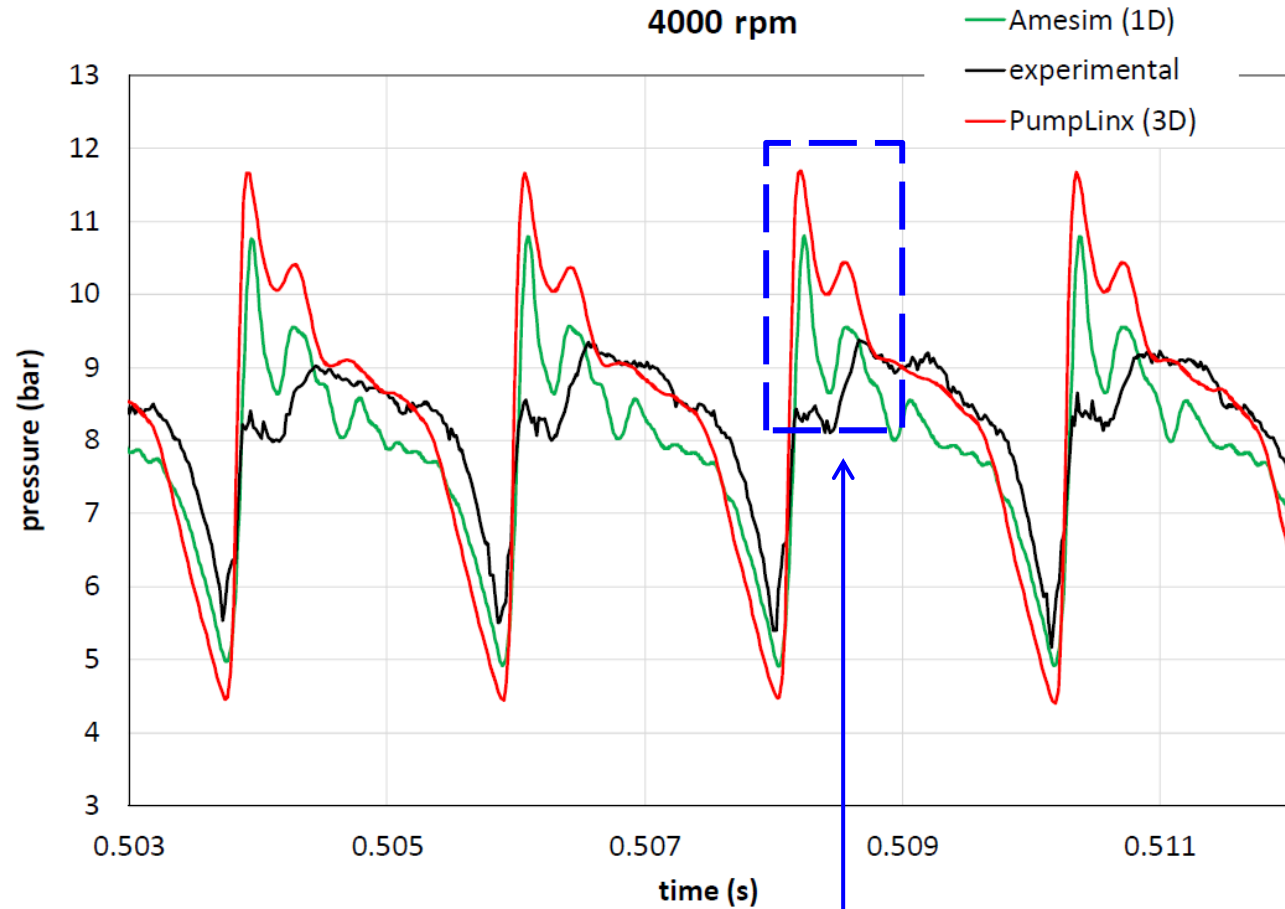
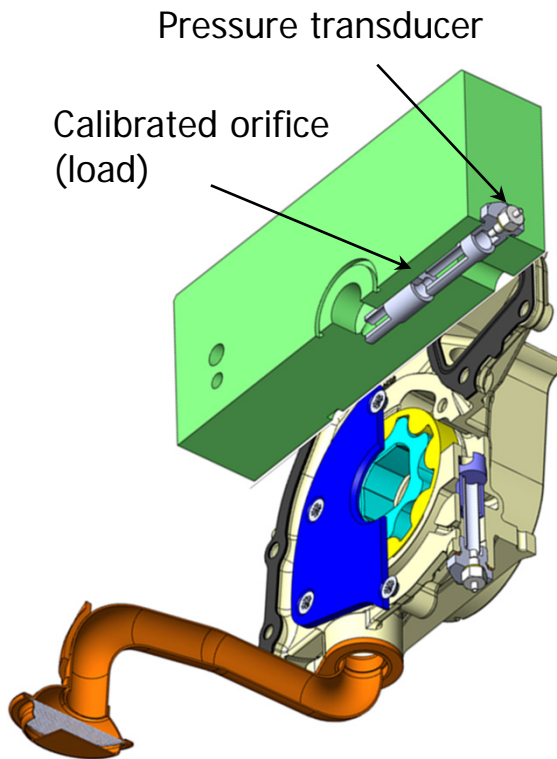
$$Q_{leak} = \frac{b(h - k \cdot p)^3}{12\mu L} p$$

gap length



# Effects on the pressure ripple (gerotor)

Simplified "short" circuit for validating the pressure ripple

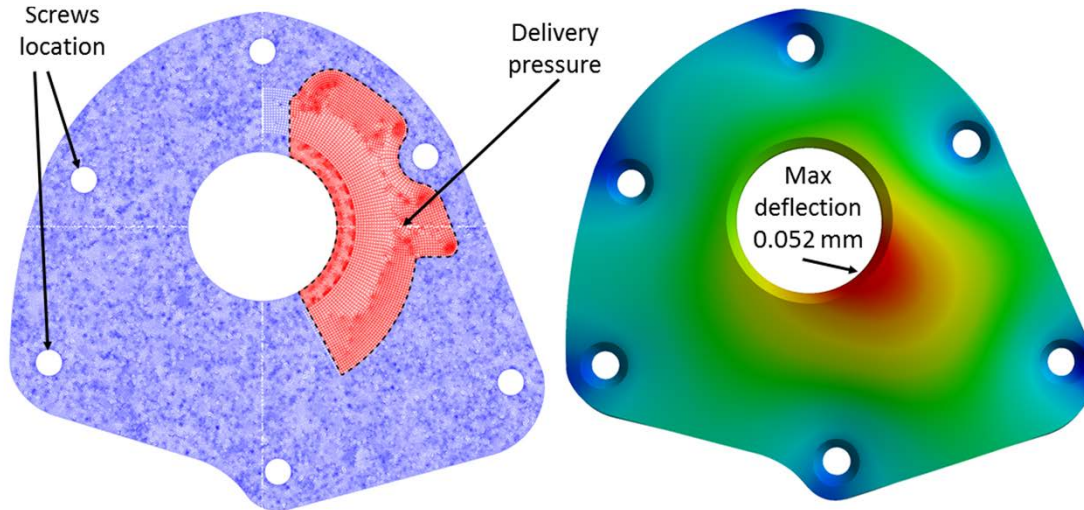


- 1D vs. 3D: very similar shape
- Exp. vs. sim. the pressure peak is missing



# Model with deformable delivery volume

Deformation field  $\delta(x, y)$



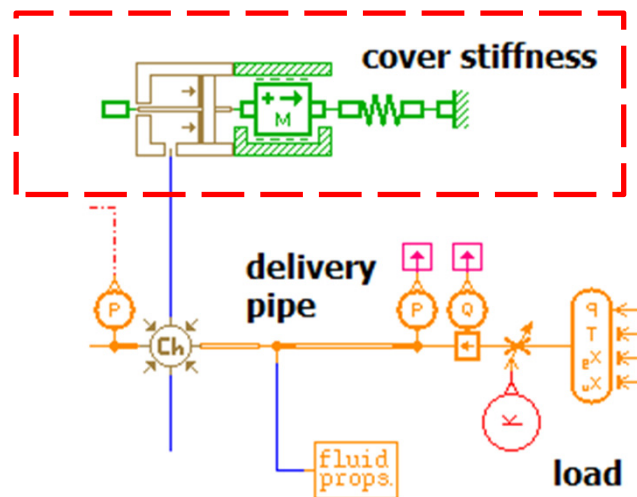
Increment of delivery volume

$$\Delta V = \int_S \delta dS$$

Equivalent spring accumulator with stiffness  $k_{eq}$

$$F = k_{eq} \Delta x = pS$$

$$k_{eq} = \frac{p \cdot S^2}{\Delta V}$$

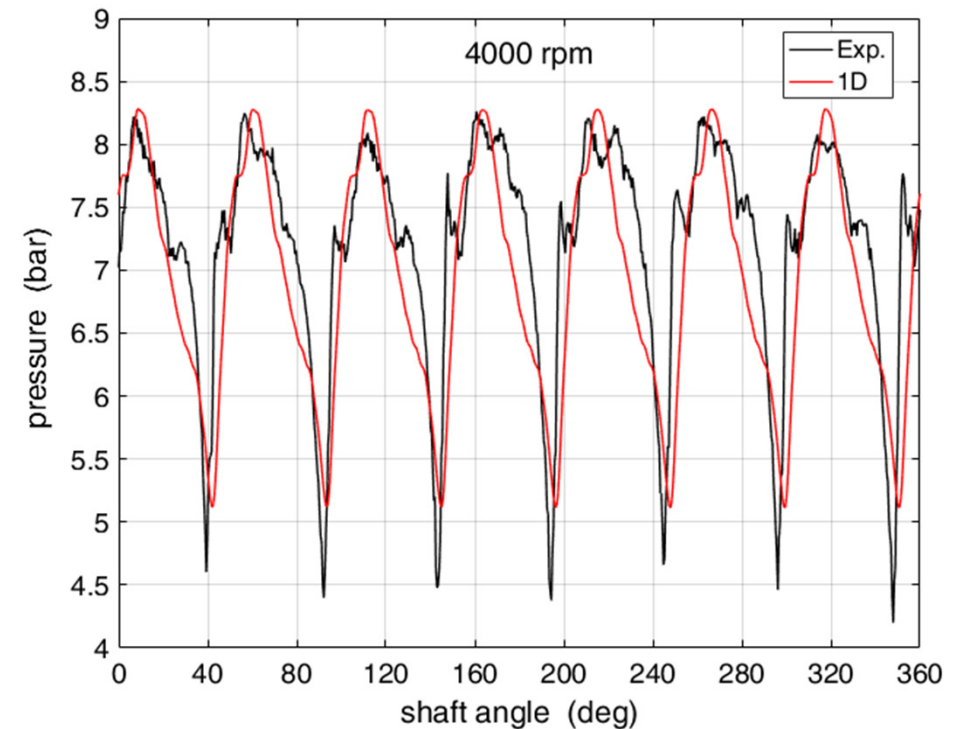
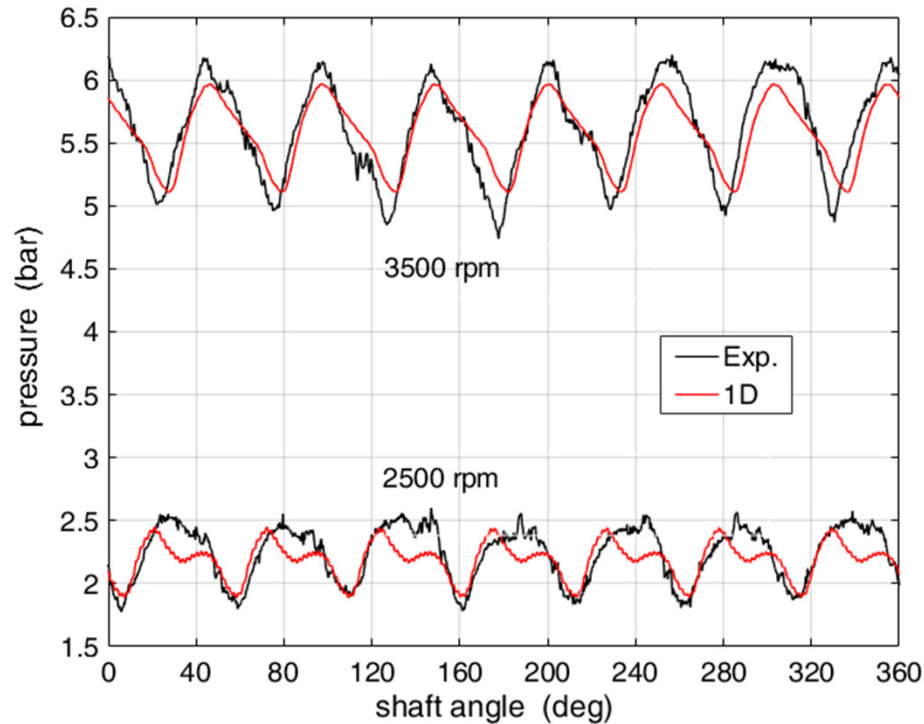


p [bar]	$\Delta V$ [mm <sup>3</sup> ]	$k_{eq}$ [kN/mm]
3	18.55	54.10
5	30.09	58.02
8.2	49.70	55.11



# Improvement of the model

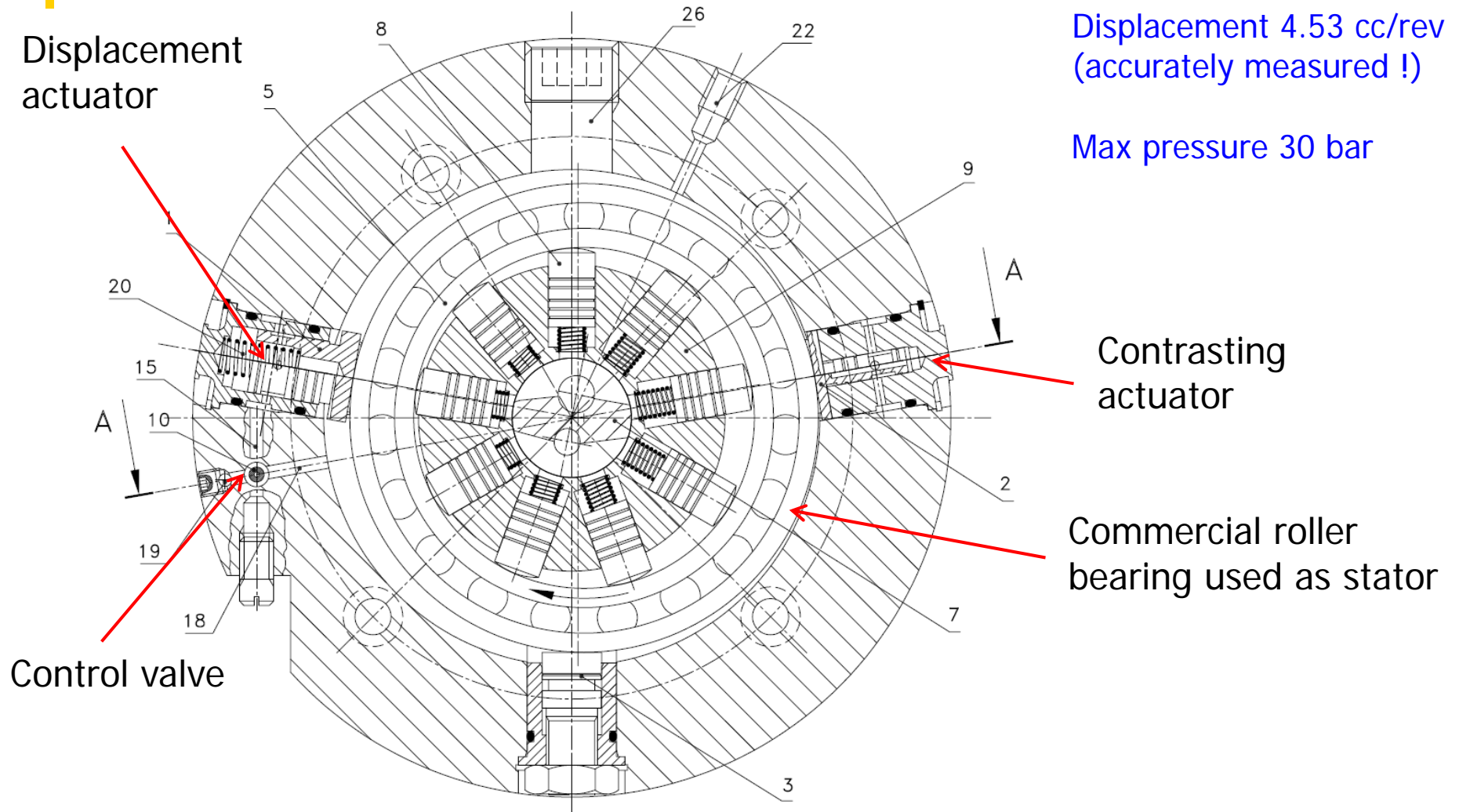
The peak has disappeared



→ Unusual aspect to be considered: **cover pulsation**



# The case of radial piston pump prototype

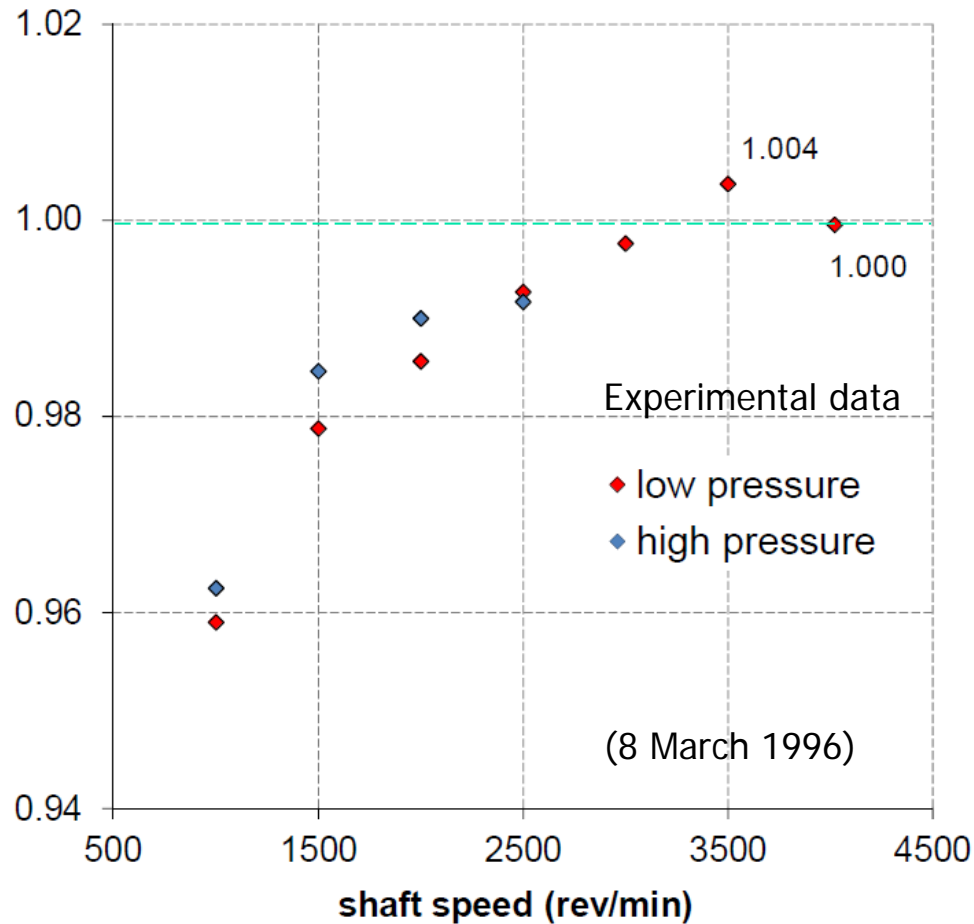


Topic of the presenter's thesis (1996)



# Very high (too much!) volumetric efficiency

Volumetric efficiency at constant pressure, temperature and displacement



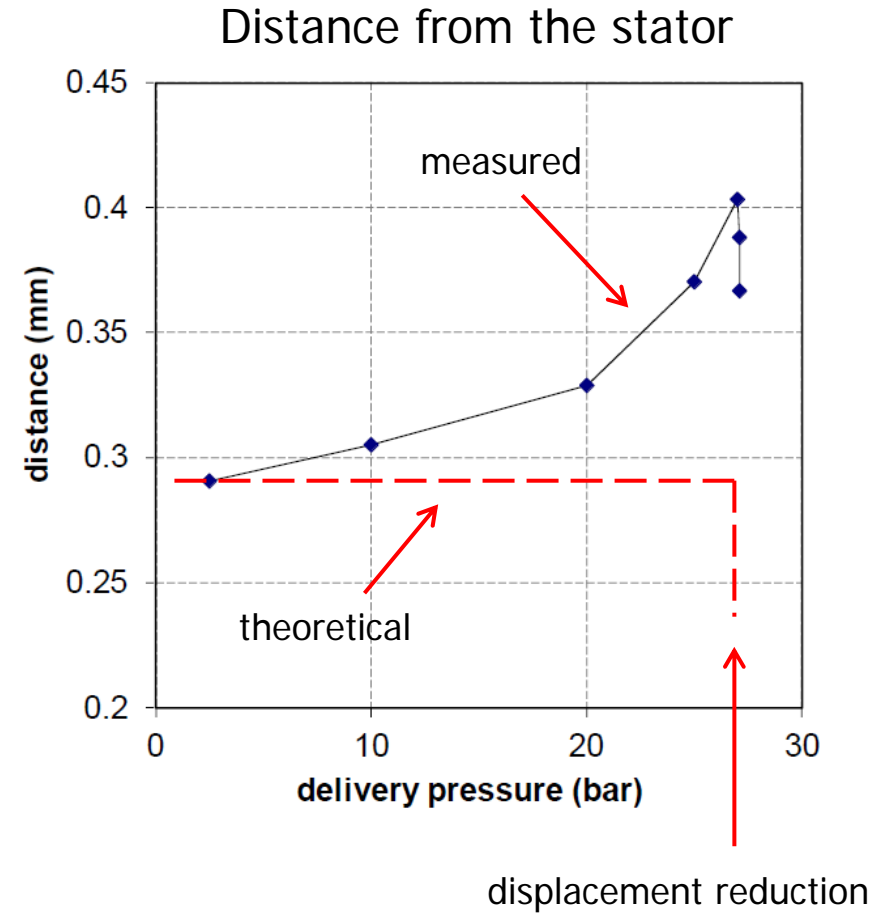
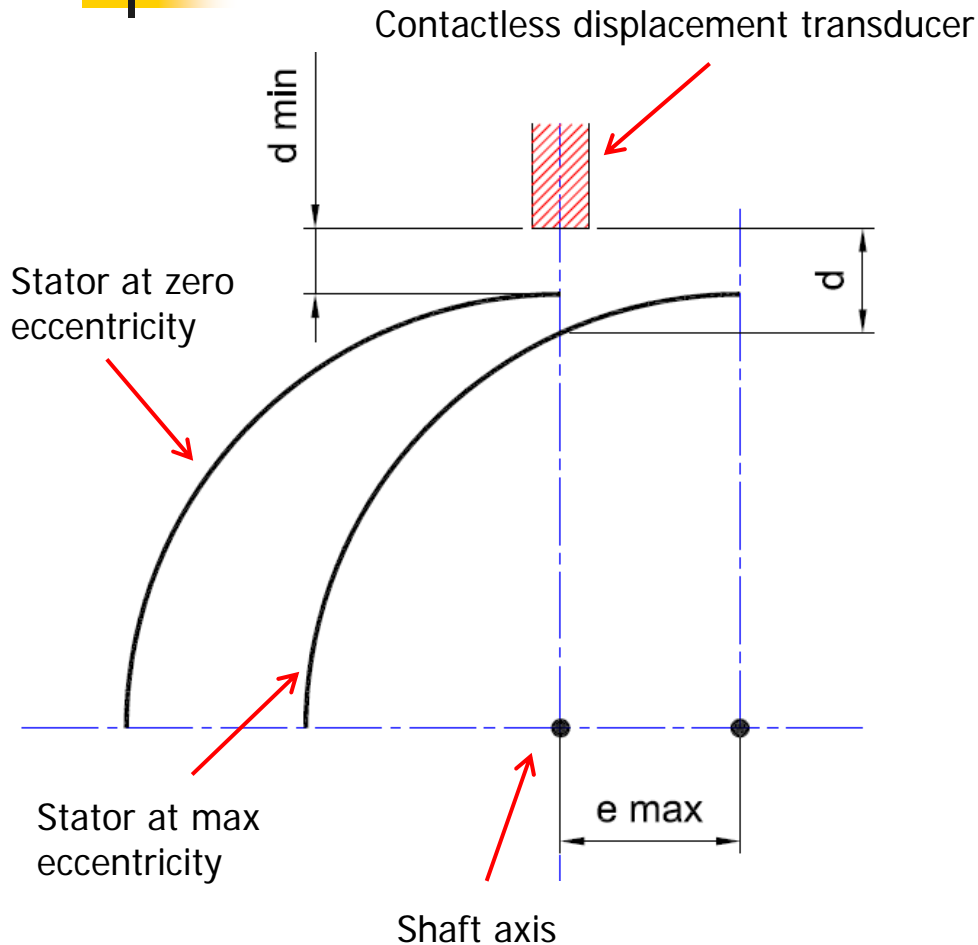
The trend is reasonable  
(increment with the speed)

but:

- values  $\geq 1$  (!)
- At equal speed, higher at high pressure



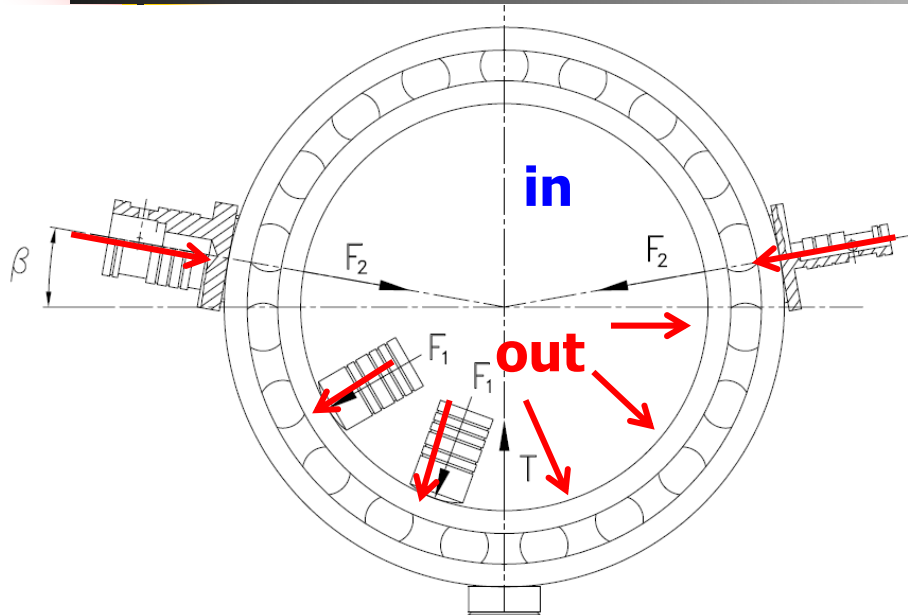
# Output of displacement transducer



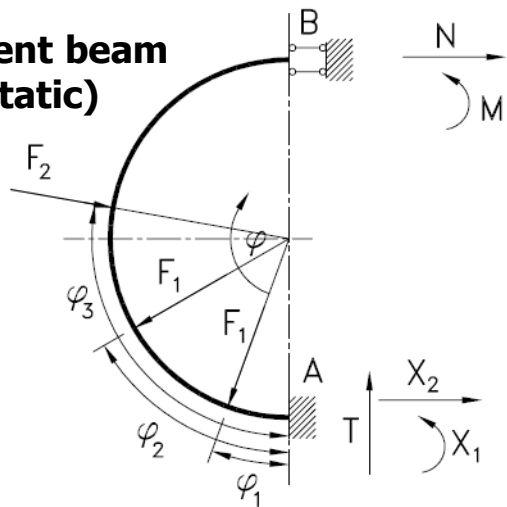
The sensor measured an increment of the distance, but it would have implied an increment of the eccentricity (impossible)



# Deformation of the stator

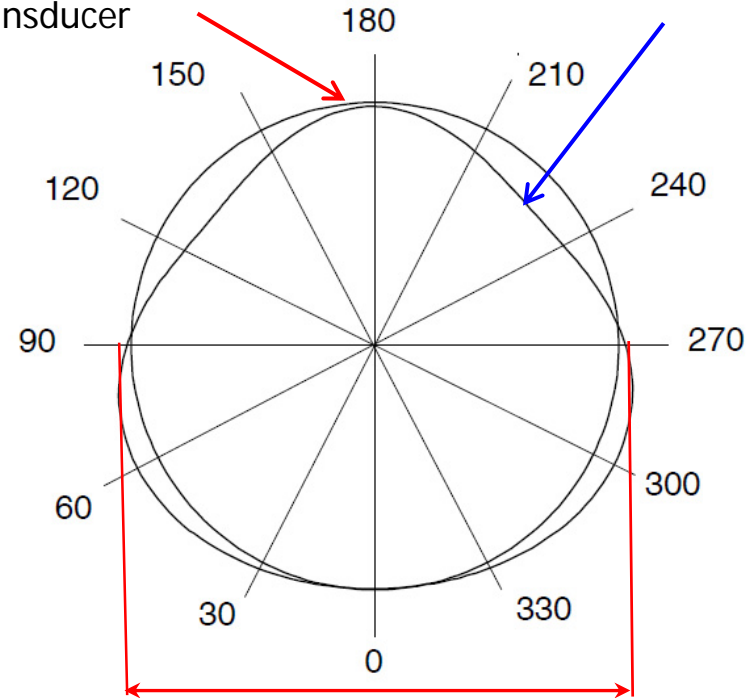


**Equivalent beam (hyperstatic)**



Increment of the distance from the transducer

**Deformed configuration**



**Increment of the pistons' stroke  
-> increment of the pump displacement**

**→ The stroke of the piston must be corrected as function of the delivery pressure**







# Conclusions

- Nothing is rigid and everything is flexible  
... even in low pressure machines !
- The “common” best practices for designing the pumps  
not “always” are the best practices

For in-depth analysis, see also:

- RUNDO M., ALTARE G., CASOLI P. "*Simulation of the Filling Capability in Vane Pumps*", Energies 12(2), 2019.
- ALTARE G., RUNDO M. "*Advances in simulation of gerotor pumps: An integrated approach*", Proc. IMechE Part C: 231(7), 2017.
- RUNDO M., PAVANETTO M.A. "*Comprehensive Simulation Model of a High Pressure Variable Displacement Vane Pump for Industrial Applications*", ASME IDETC/CIE 2018, Quebec City.
- CARETTO R., MANCÒ S., NERVEGNA N. RUNDO M. "*Modelling, Simulation and Experimental Studies on a Variable Displacement Radial Piston Pump Prototype for Automotive Applications*" ASME FPST 1996, Atlanta.

*Thank you for your kind attention*

